## Concepts and Examples Horizontal and Vertical Lines

Based on power point presentations by Pearson Education, Inc. Revised by Ingrid Stewart, Ph.D.

Learning Objectives

1. Write and graph horizontal lines.
2. Write and graph vertical lines.

## 1. The Equation of a Horizontal Line $(1$ of 3$)$

We will now discuss two equations in two variables which, at first glance, don't seem to consist of two variables.

The general form of a Horizontal Line is

$$
\boldsymbol{y}=\boldsymbol{b} \text { where } \boldsymbol{b} \text { can be any real number }
$$

There is no $x$-variable in this equation!!! However, it is still considered an equation in two variables as long as you are told that's what it is.

In this case, it is simply assumed that $x$ can take on all real values with the $\boldsymbol{b}$ being the $y$-value of all points on the horizontal line.

The graph of this equation is a horizontal line parallel to the $x$-axis where $\boldsymbol{b}$ is the $y$-intercept and the ordered pair associated with the $y$-intercept is (0, $\mathbf{b}$ ).

## The Equation of a Horizontal Line (2 of 3 )

## Example 1:

Graph the line $y=3$ by hand.
We are told that $y=3$ is a line. From the equation we know that we are dealing with a horizontal line parallel to the $x$-axis. We note that the $y$-intercept is 3 . Therefore, the ordered pair associated with this intercept is ( 0,3 ). Let's plot this ordered pair and then simply draw a horizontal line through it that is parallel to the $x$-axis.


You MUST memorize that the general equation of a horizontal line is $\boldsymbol{y}=\boldsymbol{b}$ where $\boldsymbol{b}$ can be any real number.

## The Equation of a Horizontal Line (3 of 3 )

## Example 2:

Write an equation of a horizontal line through the point created by the ordered pair $(-2,6)$.
To help is with the task, let's plot the ordered pair $(-2,6)$ and then draw a horizontal line through it that is parallel to the $x$-axis.


We know that a horizontal line has an equation of $\boldsymbol{y}=\boldsymbol{b}$, where $\boldsymbol{b}$ is the $\boldsymbol{y}$-intercept of the line. In the graph, we see that the $y$-intercept is 6 .

Therefore, the equation of the horizontal line through the point created by the ordered pair $(-2,6)$ must be $\boldsymbol{y}=6$.

## 2. The Equation of a Vertical Line ${ }_{(1 \text { of } 3)}$

The general form of a Vertical Line is

$$
\boldsymbol{x}=\boldsymbol{a} \text { where } \boldsymbol{a} \text { can be any real number }
$$

There is no $y$-variable in this equation!!! However, it is still considered an equation in two variables as long as you are told that's what it is.

In this case, it is simply assumed that $y$ can take on all real values with the $\boldsymbol{a}$ being the $x$-value of all points on the vertical line.

The graph of this equation is a vertical line parallel to the $y$-axis where $\boldsymbol{a}$ is the $x$-intercept and the ordered pair associated with the $x$-intercept is $(\mathbf{a}, \mathbf{0})$.

## The Equation of a Vertical Line (2 of 3 )

## Example 3:

Graph the line $x=3$ by hand.
We are told that $x=3$ is a line. From the equation we know that we are dealing with a vertical line parallel to the $y$-axis. We note that the $x$-intercept is 3 . Therefore, the ordered pair associated with this intercept is $(3,0)$. Let's plot this ordered pair and then simply draw a vertical line through it that is parallel to the $y$-axis.


You MUST memorize that the general equation of a vertical line is $\boldsymbol{x}=\boldsymbol{a}$ where $\boldsymbol{a}$ can be any real number.

## The Equation of a Vertical Line (3 of 3 )

## Example 4:

Write an equation of a vertical line through the point created by the ordered pair (-2, 6).
To help is with the task, let's plot the ordered pair $(-2,6)$ and then draw a vertical line through it that is parallel to the $y$-axis.


We know that a vertical line has an equation of $\boldsymbol{x}=\boldsymbol{a}$, where $\boldsymbol{a}$ is the $x$-intercept of the line.

In the graph, we see that the $x$-intercept is -2 .
Therefore, the equation of the vertical line through the point created by the ordered pair $(-2,6)$ must be $\boldsymbol{x}=\mathbf{- 2}$.

