## Examples

 The Integers
## Simple Order of Operations

Based on power point presentations by Pearson Education, Inc. Revised by Ingrid Stewart, Ph.D.

## Learning Objectives

1. Define the integers.
2. Find the absolute value of an integer.
3. Add integers.
4. Subtract integers.
5. Multiply integers.
6. Divide integers.
7. Use the calculator to perform operations on integers.
8. Use the simple Order of Operations.

## Example 1: Find Absolute Value

Find the absolute value of
a. $|-3|$
b. $|5|$
c. $|0|$
a. $|-3|=3$ because -3 is 3 units away from 0 .
b. $|5|=5$ because 5 is 5 units away from 0 .
c. $|0|=0$ because 0 is 0 units away from itself.


$$
|0|=0
$$

## Example 2: Add Integers

Evaluate -2 + (-9).

Both numbers are negative.

## Adding a gambling loss to another gambling loss is still a gambling loss.

$-2+(-9)$
$-2-9 \quad$ We eliminated the double signs!

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## Example 3: Add Integers

a. Evaluate $2+(+9)$.

Both numbers are positive. Note that a positive sign on the first number is always left off.

## Adding a gambling gain to another gambling gain is still a gambling gain.

$2+(+9)=$
$2+9 \quad$ We eliminated the double sigs!
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b. Evaluate $0+(-9)$.

## Adding a gambling loss to an already empty wallet is a loss.

Therefore, $0+(-9)$ is equal to -9 .

## Example 4: Add Integers

## Evaluate $2+(-9)$.

One number is positive and the other one negative. Note that a positive sign on the first number is always left off.

## Adding a large gambling loss to a smaller gain, we still have a gambling loss.

$2+(-9)$
2-9 We eliminated the double sigs!

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## Example 5: Add Integers

$$
\text { Evaluate - } 2+(+9)
$$

One number is positive and the other one negative.

## Adding a small gambling loss to a larger gambling gain is still a gambling gain.

$$
-2+(+9)
$$

$-2+9$
We eliminated the double signs!
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## Example 6: Subtract Integers

Evaluate 2 - (+9).
We change the operational sign from minus to plus and we change the directional sign of the subtrahend (the second number) to the opposite sign.
$2+(-9)$
Then we use gambling losses/gains to evaluate.
2-9 We eliminated the double signs!

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## Example 7: Subtract Integers

Evaluate -2-(-9).
We change the operational sign from minus to plus and we change the directional sign of the subtrahend (the second number) to the opposite sign.
$-2+(+9)$
Then we use gambling losses/gains to evaluate.
$-2+9$ We eliminated the double signs!
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## Example 8: Multiply Integers

a. Evaluate -2 - 9 .

One number is positive and the other one negative. Therefore, their product is negative.
-2. 9
-18
b. Evaluate -2 • (-9).

Both numbers are negative. Therefore, their product is positive.
$-2 \cdot(-9)$
18
Usually, we don't show the + sign.

## Example 9: Divide Integers

a. Evaluate $-9 \div(-3)$

Both numbers are negative. Therefore, their quotient is a positive 3.
b. Evaluate $9 \div(-3)$.

One number is positive and the other one negative. Therefore, their quotient is -3 .
c. Evaluate $9 \div 3$.

Both numbers are positive. Therefore, their quotient is a positive 3.
d. Evaluate $-9 \div 3$.

One number is positive and the other one negative. Therefore, their quotient is -3 .

## Example 10: Use the Simple Order of Operations

a. Evaluate $18 \div(-9) \cdot 3$.

There is only division and multiplication. We work from left to right.

```
18\div(-9)\cdot3
-2.3
-6 (evaluated the multiplication)
```

b. Evaluate - $2 \cdot 9 \cdot(-3)$.

There is only multiplication. We work from left to right.

```
-2.9.(-3)
    -18\cdot(-3) (evaluated the first multiplication)
54 (evaluated the second multiplication)
```


## Example 11: Use the Simple Order of Operations

Evaluate 6-24+4-3+1.
There is only addition and subtraction. We work from left to right.
$6-24+4-3+1$
$-18+4-3+1$ (evaluated the subtraction)
$-14-3+1 \quad$ (evaluated the addition)
$-17+1 \quad$ (evaluated the subtraction)
-16 (evaluated the addition)
Note, in the case of addition and subtraction, it is not necessary to observe the Order of Operations.

## Example 12: Use the Simple Order of Operations

Evaluate $36-24 \div 4 \cdot 3+1$.

There is addition, subtraction, multiplication, and division. We begin by evaluating the division. Remember, multiplication and division are done before addition and subtraction working from left to right.
$36-24 \div 4 \cdot 3+1$
$36-6 \cdot 3+1 \quad$ (evaluated the division)
36-18+1 (evaluated the multiplication)
$18+1$ (evaluated the subtraction)
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(evaluated the addition)

