



PROBLEMS AND SOLUTIONS - SOLVING EXPONENTIAL EQUATIONS
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Please Send Questions and Comments to ingrid.stewart@csn.edu. Thank you!

PLEASE NOTE THAT YOU CANNOT ALWAYS USE A CALCULATOR ON THE ACCUPLACER - COLLEGE-LEVEL MATHEMATICS TEST! YOU MUST BE ABLE TO DO SOME PROBLEMS WITHOUT A CALCULATOR!

Problem 1:

Solve $10^x = 5.71$. Round to 4 decimal places.

Problem 2:

Solve $7e^x = 15$. Round to 4 decimal places.

Problem 3:

Solve $16^{x-4} = \frac{1}{2}$.

Problem 4:

Solve $9^{2x} = 27^{x+1}$ not using logarithms!

Problem 5:

Solve $5^{x-2} = 3^{2x+1}$. Round to 3 decimal places.

Problem 6:

How many years will it take for an initial investment of **\$10,000** to grow to **\$25,000**? Assume a rate of interest of **2.5%** compounded continuously. Round your answer to a whole number. Use the formula $A = Pe^{rt}$, where **P** is the initial investment, **A** is the accumulated amount, **t** is the time in years and **r** is the interest rate in decimals.

Problem 7:

The number of bacteria **A** in a certain culture is given by the growth model $A = 250e^{kt}$. Find the growth constant **k** knowing that **A = 280** when **t = 5**. Round your answer to four decimal places.

Problem 8:

The half-life of a radioactive substance is **950 years**. Find the constant **k** rounded to seven decimal places. Do not use scientific notation! Hint: Half-life means that exactly one-half of the original amount or size of the substance is left after a certain number of

years of growth/decay. Use the *Exponential Growth/Decay Model* $A = A_0 e^{kt}$, where A_0 is the original amount, A is the accumulated amount, t is the time in years and k is the growth constant.

Problem 9:

The next problem involves carbon-14 dating which is used to determine the age of fossils and artifacts. The method is based on considering the percentage of a half-life of carbon-14 of approximately 5715 years. Specifically, the model for carbon-14 is

$$A = A_0 e^{-0.000121 t}$$

In 1947, an Arab Bedouin herdsman found earthenware jars containing what are known as the Dead Sea scrolls. Analysis at that time indicated that the scroll wrappings contained 76% of their original carbon-14. Estimate the age of the scrolls in 1947. Round your answer to a whole number.



SOLUTIONS

You can find detailed solutions below the link for this problem set!

1. $x \approx .7566$	2. $x \approx .7621$	3. $x = \frac{3}{4} = .75$
4. $x = 3$	5. $x \approx -7.345$	6. $t \approx 37$
7. $k \approx 0.0227$	8. $k \approx -0.0007296$	9. 2,268 years old