

$$\lim_{x \rightarrow \infty} \int_2^3 \frac{1}{dx} dy$$

## THE DERIVATIVE

Prepared by Ingrid Stewart, Ph.D., College of Southern Nevada  
Please Send Questions and Comments to [ingrid.stewart@csn.edu](mailto:ingrid.stewart@csn.edu). Thank you!

### Problem 1:

Given  $f(x) = 3x^2 + 4x - 5$ , find  $f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$ .

### Problem 2:

Differentiate the function  $f(x) = x - x^2$ .

### Problem 3:

Find the derivative of  $f(x) = \frac{1}{x^2}$ .

### Problem 4:

Find the instantaneous rate of change of the function  $f(x) = \sqrt{x}$ .

### Problem 5:

a. Find the slope of the line tangent to the point  $(-1, 2)$  on the function  $f(x) = x^3 - 3x$  using the *Difference Quotient*  $\frac{f(x+h) - f(x)}{h}$ .

b. Find the slope of the line tangent to the point  $(-1, 2)$  on the function  $f(x) = x^3 - 3x$  using the alternative form of the derivative, that is,  $f'(c) = \lim_{x \rightarrow c} \frac{f(x) - f(c)}{x - c}$ .

### Problem 6:

Find the equation of the line tangent to the point  $(-1, 2)$  on the function  $f(x) = x^3 - 3x$ . See Problem 5 above!



## SOLUTIONS

You can find detailed solutions below the link for this problem set!

1. $6x + 4$	2. $1 - 2x$	3. $\frac{-2}{x^3}$
4. $\frac{1}{2\sqrt{x}}$	5. $0$	6. $y = 2$