

$$\lim_{x \rightarrow \infty} \int_2^3 \frac{1}{dx} dy$$

## SOME BASIC DIFFERENTIATION RULES

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### Problem 1:

Find the derivative of the following functions:

a.  $f(x) = -4x^{5/4}$

b.  $f(x) = 6 - x + 2x^3 - 4x^6$

c.  $f(x) = -2x^3 - \sqrt[3]{x^5}$

d.  $f(x) = x^{4/3}(x^2 + 3x^{2/3} - 6)$

e.  $f(x) = (2x - 3)^2$

f.  $f(x) = (x^3 - 2)(2x + 1)$

### Problem 2:

Differentiate the following functions. Write any negative exponents in your answer as fractions and then write as a SINGLE fraction, if necessary.

a.  $f(x) = x^3 + \frac{1}{x}$

b.  $f(x) = (4x)^{-2}$

c.  $f(x) = \frac{3x^2 - 7x + 2}{x}$

d.  $f(x) = \frac{4x^3 + 5x - 9}{2}$

e.  $f(x) = \frac{3\sqrt{x}}{x}$

f.  $y = \frac{4x^2 - 5}{x^3}$

**Problem 3:**

Find the slope-intercept equation of the line tangent to the graph of  $f(x) = 2x - 3x^{1/2}$  at the point  $(9,9)$ .

**Problem 4:**

Find the first, second derivative, and third derivatives of the following functions:

a. Given  $f(x) = -2x^{6/5}$

b. Given  $y = 3x - 1$


**SOLUTIONS**

You can find detailed solutions below the link for this problem set!

1.a. $f'(x) = -5x^{1/4}$	1.b. $f'(x) = -1 + 6x^2 - 24x^5$	1.c. $f'(x) = -6x^2 - \frac{5}{3}x^{2/3}$
1.d. $f'(x) = \frac{10}{3}x^{7/3} + 6x - 8x^{1/3}$	1.e. $f'(x) = 8x - 12$	1.f. $f'(x) = 8x^3 + 3x^2 - 4$
2.a. $f'(x) = \frac{3x^4 - 1}{x^2}$	2.b. $f'(x) = \frac{-1}{8x^3}$	2.c. $f'(x) = \frac{3x^2 - 2}{x^2}$
2.d. $f'(x) = \frac{12x^2 + 5}{2}$	2.e. $f'(x) = \frac{-3}{2x^{3/2}}$	2.f. $\frac{dy}{dx} = \frac{-4x^2 + 15}{x^4}$
3. $y = \frac{3}{2}x - \frac{9}{2}$	4.a. $f'(x) = -\frac{12}{5}x^{1/5}$ $f''(x) = -\frac{12}{25}x^{-4/5}$ $f'''(x) = \frac{48}{125}x^{-9/5}$	4.b. $\frac{dy}{dx} = 3$ $\frac{d^2y}{dx^2} = 0$ $\frac{d^3y}{dx^3} = 0$